

# Selection of pneumatic control valves from catalogues<sup>†</sup>

Tomasz Kiczkowiak\*

*Institute of Mechatronics, Nanotechnology and Vacuum Technique, Koszalin University of Technology  
Raclawicka 15–17, 75–620 Koszalin, Poland*

(Manuscript Received July 24, 2007; Revised October 30, 2008; Accepted April 25, 2009)

---

## Abstract

In a case of computer simulation used for the verification of pneumatic system performance, one of the main problems is that various parameters can be used to describe flow characteristics of the system components. Although the Standard ISO 6358 offers two parameters: the sonic conductance  $C$  and the critical static pressure ratio  $b$ , these cannot be directly utilised in the selection of elements comprising a pneumatic system. In this paper, we present two algorithms for calculating the volumetric flow rate  $Q_V$  and the flow coefficient  $K_V$  as a function of sonic conductance  $C$  and critical pressure ratio  $b$  (recommended by the standard) toward the improved selection of pneumatic control valves.

*Keywords:* Flow characteristics; Flow coefficient; Pneumatic control valves; Volumetric airflow rate

---

## 1. Introduction

During a selection of pneumatic control valves from vendors' catalogues, some calculations are conducted. The main goal of such calculations is to determine the parameters describing flow characteristics of the valves. The flow characteristics [1] can be described by [2]:

- armature nominal diameter  $d_k$ ;
- volumetric airflow rate in normal conditions  $Q_{Nnom}^1$ ;
- flow coefficient  $K_V$  according to the standard VDI/VDE 2173 [3];
- sonic conductance  $C$  and critical pressure ratio  $b$  [4]; and
- air – flow coefficient  $\mu$  [5].

<sup>1</sup> For the overpressure before element  $p_{nom} = 600\,000$  Pa and the pressure drop  $\Delta p_{nom} = 100\,000$  Pa.

<sup>†</sup> This paper was recommended for publication in revised form by Associate Editor Jun Sang Park

\*Corresponding author. Tel.: +4894 3478 388, Fax.: +4894 3478 489  
E-mail address: tomasz.kiczkowiak@tu.koszalin.pl

© KSME & Springer 2009

Of these, only the first three are utilised in traditional algorithms of calculations. The parameters applied depend on the algorithm that has been selected [2]. According to [2, 6], the sonic conductance  $C$  and the critical pressure ratio  $b$  should be utilised because:

- two parameters can more precisely describe flow properties;
- they are proposed by a currently valid standard (ISO 6358);
- some parameters determined by algorithms of calculations (e. g., armature nominal diameter  $d_k$ ) are not strictly connected with flow properties of a pneumatic element, and only a reluctance to try new methods is the reason why they can be found in the vendors' catalogues; and
- they can be converted into other coefficients (e. g., an air – flow coefficient  $\mu$  [5]) and, thanks to that, they can be used for pneumatic system analysis.

## 2. Problem formulation

In 1989, the ISO 6358 [4] standard that was introduced described the flow parameters of pneumatic

devices. It defined two flow parameters: a sonic conductance  $C$  and a critical (static) pressures rate  $b$ ; the same standard also described the appropriate determination and application methods. The parameters are suitable for comparing the flow properties of two pneumatic elements.

According to the standard ISO 6358 [4], the sonic conductance, the critical pressure ratio, the critical flow, and the mass flow rate are defined as follows:

**The sonic conductance  $C$**  is defined as the ratio of the mass flow  $\dot{m}$  through the element to the product of the input gas pressure  $p_1$  as well as its density  $\rho_N$ , in the standard conditions ANR<sup>2</sup>, for the critical flow:

$$C = \frac{\dot{m}}{p_1 \cdot \rho_N} \quad (1)$$

**The critical pressure ratio  $b$**  is the maximal value of  $p_2/p_1$ , at which the critical flow occurs.

**The critical flow** is a situation during which the flow in some sub-space of an element is equal to the local sound velocity. It occurs when the inlet pressure  $p_1$  is sufficiently high in comparison to the outlet pressure  $p_2$ . The mass flow is then seen as proportional to the inlet pressure  $p_1$  and inversely proportional to the root square of the inlet stream temperature  $T_1$ . At the same time, it does not depend upon the outlet pressure  $p_2$ .

The **mass flow rate** of air is described by the formula:

$$\dot{m} = \frac{p_1}{\sqrt{T_0}} \cdot \rho_N \cdot \sqrt{T_N} \cdot H, \quad (2)$$

where

$$H = \begin{cases} C & \text{for } p_2/p_1 \leq b \\ C \cdot \sqrt{1 - \left(\frac{p_2/p_1 - b}{1 - b}\right)^2} & \text{for } b < p_2/p_1 \leq 1 \end{cases} \quad (3)$$

Although the ISO standard has been enforced 15 years ago, only few vendors present values of  $C$  and  $b$  in their catalogues [4]. There are two reasons behind this.

- (1) An experimental determination of the sonic conductance and the critical pressure ratio according to ISO 6358 standard is very difficult, especially

for elements with good flow properties and large diameters.

- (2) There is a lack of algorithms that could make it possible to calculate these parameters on the basis of requirements for a pneumatic system.

For many years, previous works have been carried out on CAD systems for pneumatic driving systems at the Koszalin University of Technology. Selection of pneumatic devices from the vendors' catalogues is an important problem in such systems. As a solution, a previous study highlighted the possibility of using Artificial Neural Networks to augment the calculation of control valves parameters [7]. In this paper, we propose another approach to solve this problem.

Although methods of determining flow parameters as a function of  $C$  and  $b$  have been presented in [2], there are no methods in the opposite direction. This is the main reason why the reverse task has been formulated:

*for the knowing value of a flow parameter (e. g., the flow coefficient  $K_V$ ) the values of  $C$  and  $b$  must be determined to make catalogue selection possible.*

The task has no direct solution because two values must be calculated from one known parameter. Below, we present the methods of determination of  $C$  and  $b$  from  $Q_{Nnom}$  or  $K_V$ .

### 3. Determination of the sonic conductance $C$ and the critical pressure ratio $b$ from the nominal volumetric flow rate $Q_{Nnom}$

The relation between the volumetric flow rate  $Q$  [m<sup>3</sup>/h] and the mass flow rate  $\dot{m}$  [kg/s] in the same conditions is given by:

$$Q = \dot{m} \cdot \frac{3600}{\rho} \quad (4)$$

Inserting (3) into (4), in case of the nominal flow in the standard conditions  $Q_N$  [m<sup>3</sup>/h], the relation among the flow value, the sonic conductance value  $C$  [m<sup>4</sup>·s/kg], the critical pressure ratio value  $b$ , and the pressure ratio  $Y$  are thus obtained:

$$Q_N = 3600 \cdot C \cdot p_1 \cdot \sqrt{\frac{T_N}{T_0}} \quad (5)$$

for  $Y \leq b$  or by:

<sup>2</sup> ANR – the standard conditions ( $p_N=100000$  Pa,  $T_N=293.15$  K)

$$Q_N = 3600 \cdot C \cdot p_1 \cdot \sqrt{\frac{T_N}{T_0}} \cdot \sqrt{1 - \left(\frac{Y-b}{1-b}\right)^2} \tag{6}$$

for  $Y > b$ .

A pressure ratio  $Y$  can be defined by:

$$Y = \frac{p_2}{p_1} = 1 - \frac{\Delta p}{p_{\text{inad}} + p_a} \tag{7}$$

For the nominal flow  $Q_{Nnom}$ , when  $\Delta p = \Delta p_{nom} = 100\,000$  Pa,  $p_{\text{inad}} = p_{\text{inad}} = 600\,000$ , and  $p_a = 100\,000$  Pa we obtain from (7) the pressure ratio  $Y_{def} = 6/7 \approx 0.8571$ . In such a case when  $b > Y_{def}$ , from relation (5),  $C$  is given by:

$$C = C_{min} = \frac{1}{3600 \cdot 700000} \cdot Q_{Nnom} \cdot \sqrt{\frac{T_0}{T_N}} = 3.968 \cdot 10^{-10} \cdot Q_{Nnom} \cdot \sqrt{\frac{T_0}{T_N}} \tag{8}$$

In the opposite case when  $b < Y_{def}$ , from relation (6),

$$C = 3.968 \cdot 10^{-10} \cdot Q_{Nnom} \cdot \sqrt{\frac{T_0}{T_N}} \cdot \frac{1}{\sqrt{1 - \left(\frac{Y_{def}-b}{1-b}\right)^2}} = C_{min} \cdot \frac{1}{\sqrt{1 - \left(\frac{Y_{def}-b}{1-b}\right)^2}} = C_{min} \cdot W(b) \tag{9}$$

For  $b = 0$ , the sonic conductance equals  $1.9412 \cdot C_{min}$ . Below (Fig. 1, Table 1), the values of coefficients increasing a sonic conductance for the various pressure ratios are presented.

Having known the value of  $Q_{Nnom}$  in normal conditions, the valve selection procedure is as follows:

- (1) Determine the minimal value of a sonic conductance  $C_{min}$  using Eq. (8).
- (2) Find a valve with  $b \geq 0.8571$  and  $C \geq C_{min}$ .
- (3) If the pressure rate  $b$  of the valve is less than 0.8571 then one should look for a valve with the sonic conductance  $W(b)$  (Fig. 1, Table 1) times greater than the minimal one ( $C \geq C_{min} \cdot W(b)$ ). The valve that ought to be selected must have the nominal flow rate in normal conditions no less than the required one.

Table 1. Value of the multiplicand  $W(b)$  increasing minimal sonic conductance  $C_{min}$  as function of the critical pressure ratio  $b$  for  $Y_{def} = 0.8571$ .

| $b$    | 0      | 0.1    | 0.2    | 0.5    | 0.7    | 0.85   |
|--------|--------|--------|--------|--------|--------|--------|
| $W(b)$ | 1.9412 | 1.8495 | 1.7532 | 1.4287 | 1.1738 | 1.0011 |

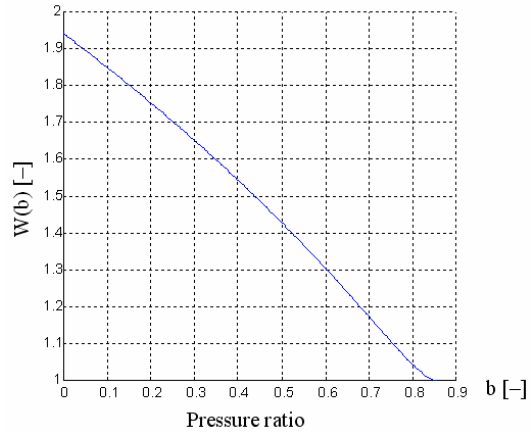


Fig. 1. Dependence of the multiplicand  $W(b)$  increasing minimal sonic conductance  $C_{min}$  as a function of the critical pressure ratio  $b$  for  $Y_{def} = 0.8571$ .

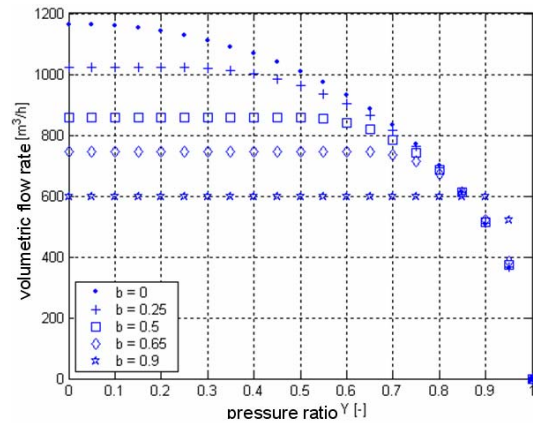


Fig. 2. Dependence of the volumetric flow rate  $Q_N$  on the pressure ratio  $Y = p_2/p_1$  for control valves with different values of  $C$  and  $b$ , and the same value of  $Q_{Nnom} = 600$  [m³/h].

The proposed method results in the selection of valves with various  $C$  and  $b$ , but always with the same value of a nominal volumetric flow rate  $Q_{Nnom}$ . The volumetric flow rate  $Q_N$ , as a function of the pressure ratio  $Y$  for the selected valves with the nominal volumetric flow rate  $Q_{Nnom} = 600$  m³/h, is presented in Fig. 2. This is represented by a set of lines crossing each other at point  $Y_{def} = 0.8571$ .

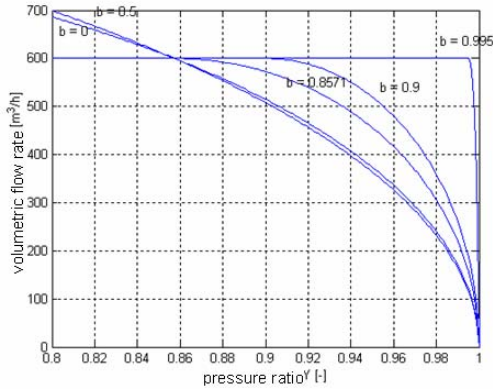


Fig. 3. Dependence of the volumetric flow rate  $Q_V$  on the pressure ratio  $Y = p_2/p_1$  ( $Y > 0.8$ ) for control valves with different values of  $C$  and  $b$ , and the same value of  $Q_{Nom} = 600$  [m<sup>3</sup>/h].

**4. Determination of the sonic conductance  $C$  and the critical pressure ratio  $b$  from the flow coefficient  $K_v$**

The value of a coefficient  $K_V$  [m<sup>3</sup>/h] as a function of a sonic conductance  $C$  [m<sup>4</sup>·s/kg] and a critical pressure rate  $b$  may be given by [4]:

$$K_v = 1.241 \cdot 10^7 \cdot C \cdot \frac{\sqrt{1 - \left(\frac{Y-b}{1-b}\right)^2}}{\sqrt{Y \cdot (1-Y)}} \quad (10)$$

If  $Y < b$  then  $Y = b$  in the numerator of (10), and if  $Y < 0.5$  then  $Y = 0.5$  in the denominator of (10).

Assigning:

$$\frac{1}{Z(b)} = \frac{\sqrt{1 - \left(\frac{Y-b}{1-b}\right)^2}}{\sqrt{Y \cdot (1-Y)}} \quad (11)$$

and transforming in order to determinate a sonic conductance, we obtain:

$$C = \frac{K_v}{1.241 \cdot 10^7} \cdot Z(b) = 0.8058 \cdot 10^{-7} \cdot K_v \cdot Z(b) \quad (12)$$

Let us assume that  $Y = 0.8571$ . For  $b \geq Y$  the value of the parameter  $Z(b)$  is  $Z(b \geq Y)_{Y=0.8571} = 0.35$ . The value  $b = 0$  produces  $Z(b=0)_{Y=0.8571} = 0.6794$ . In the analysed case ( $Y = 0.8571$ ), a change from  $b = Y$  to  $b = 0$  causes an increase of the sonic conductance by  $Z(0)_{Y=0.8571}/Z(0.8571)_{Y=0.8571} = 1.9411$ .

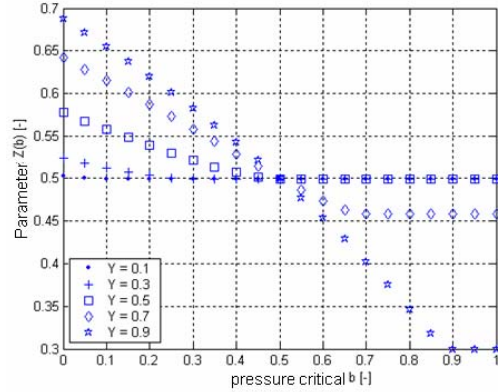


Fig. 4. Dependence of the parameter  $Z(b)$  on the pressure critical ratio  $b$  for various values of  $Y$ .

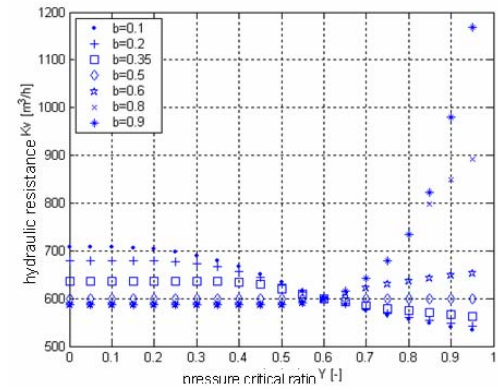


Fig. 5. Dependence of the hydraulic resistance coefficient  $K_v$  on the pressure ratio  $Y$  for different devices selected from catalogue ( $Y_{ele} = 0.6$ ). Required  $K_v = 600$  m<sup>3</sup>/h.

The same increase of sonic conductance  $C$  was obtained for the analysed problem of a nominal volumetric flow rate  $Q_{Nom}$  (section 3). The value of  $Z(b)$  as function of the critic pressure rate  $b$  for various pressure ratios  $Y$  is shown in Fig. 4 below.

Having known the value of the  $K_v$  coefficient, the valve selection procedure is as follows:

- (1) Assume the value of pressure ratio  $Y_{ele}$ .
- (2) Determine the value of a coefficient  $Z(b)_{Y=Y_{ele}}$  using Eq. (11).
- (3) Determine the minimal value of a sonic conductance  $C_{min}$  using Eq. (12).
- (4) Look for the valve with  $b \geq Y_{ele}$  and  $C > C_{min}$ . If the value of a critical pressure ration is less than the assumed one ( $b < Y_{ele}$ ), then the valve selected must have a higher value of a sonic conductance. The value can be determined from (11); the value of coefficient  $Z(b)$  from Eq. (10).

The proposed method thus results in the selection of valves with various  $C$  and  $b$  (depending on the  $Y_{ele}$  assumed), but always with the same value of a flow coefficient  $K_v$ .

## 5. Final remarks

In this paper, we presented two methods used to determine the sonic conductance  $C$  and the critical pressure ratio  $b$ , when the flow coefficient  $K_v$  or the nominal air – flow rate  $Q_{Nnom}$  are known. For both approaches, the selected valve has the value of  $K_v$  or  $Q_{Nnom}$  that is no less than the required one. Among its advantages, the proposed approach enables a selection of the pneumatic control valve from a catalogue when the sonic conductance  $C$  and the critical pressure ratio  $b$  are given but not the flow coefficient  $K_v$  or the nominal air – flow rate  $Q_{Nnom}$ , after which the traditional methods of calculation and selection can be utilized; moreover, it also allows for an interconnection of pneumatic system synthesis and analysis. To date, the parameters applied in the traditional calculation algorithms ( $K_v$  or  $Q_{Nnom}$ ) could not be converted into the air – flow coefficient  $\mu$  [5]. Now, it can be achieved through two steps: from  $K_v$  or  $Q_{Nnom}$  into  $C$  and  $b$ , (thanks to the proposed algorithms) and next  $C$  and  $b$  into  $\mu$  [6].

## References

- [1] S.-C. Baek and S.-B. Kwon, Study of Moist Air Flow Through the Ludwig Tube, *KSME International Journal*, Vol. 17 No. 12 (2003) 2066–2077.
- [2] J. Iwaszko, *Pressure loss in pneumatic components*, Prace naukowe, Mechanika Z.177, Oficyna

Wydawnicza Politechniki Warszawskiej, Warszawa, Poland (1999).

- [3] VID/VDE 2173 Richtlinien: *Strömungstechnische Kenngrößen von Stellventilen und deren Bestimmung*.
- [4] ISO 6358, *Pneumatic fluid power – Components using compressible fluids – Determination of flow – rate characteristics*, (1989).
- [5] E. W. Gerc, *Dynamics of pneumatic systems*, Maszynostrojenie, Moscow, Russian (1985).
- [6] Sz. Grymek and T. Kiczowskiak, Conversion of the sonic conductance  $C$  and the critical pressure ratio  $b$  into the airflow coefficient  $\mu$  *Journal of Mechanical Science and Technology (The Korean Society of Mechanical Engineers)*. 19 (9) (2005) 1706–1710.
- [7] Sz. Grymek and T. Kiczowskiak, Application of ANN to the Selection of a Valve from the Catalogue, [In:] L. Niklasson, M. Boden, Ziemke (Eds): *ICANN 98*, Springer-Verlag series: *Perspectives in Neural Computing*. London, 2 (1998).



**Tomasz Kiczowskiak** received his M.S. degree in Mechanical Engineering from Koszalin University of Technology, Poland, in 1978. In 1991, he received his Ph.D. degree from Warsaw University of Technology, Poland. In 2006, he received his D.Sc. degree from KUT. Dr. Kiczowskiak is currently a Professor at the Institute of Mechatronics, Nanotechnology, and Vacuum Technique of KUT in Koszalin, Poland. His research interests include mechatronics, pneumatics, CAD, and artificial intelligence applications.